

12. For permissible real values of x, y, z , the value of the expression

$$\frac{(2x+5y-3z)^3 + (2x-5y+3z)^3 + 2x(2x+5y-3z)(2x-5y+3z)}{x^3}$$
 is

- a) 16 b) 32 **c) 64** d) 128

13. When $\theta \neq 0^\circ, 90^\circ$ the value of the expression

$$\frac{(1 + \sec \theta + \tan \theta)(1 + \operatorname{cosec} \theta + \cot \theta)}{1 + \tan \theta + \cot \theta + \sec \theta + \operatorname{cosec} \theta}$$
 is equal to

- a) 1 **b) 2** c) -1 d) $\frac{1}{2}$

14. The number of real ordered pairs (x, y) which satisfy

$$4^{\frac{x+y}{y}} = 32, \text{ and } \log_3(x-y) = 1 - \log_3(x+y)$$
 is

- a) 0 **b) 1** c) 2 d) 3

15. a, b are natural numbers such that $\frac{a}{b} + \frac{b}{a} = a + b$; then

- a) a is odd and b is even.
 b) a, b are both even.
 c) Such natural numbers a and b do not exist.

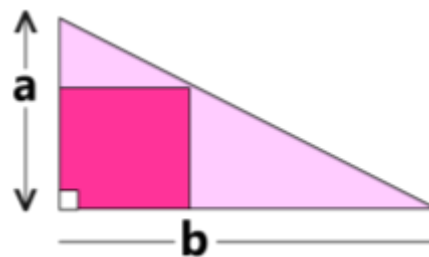
- d) There is exactly one value of 'a' and 'b' which satisfy the equation.**

Fill in the blanks:

16. The sum of all the roots of the equation $3^{\frac{x+2}{3x-4}} - 7 = 2 \left(3^{\frac{5x-10}{3x-4}} \right)$ is **2**.

17. A square is inscribed in a right angled Triangle as shown in the figure. One leg of the triangle is twice the other.

If the perimeter of the square is 64 cm, then the length of longer leg of the triangle (in cm) is **48**.



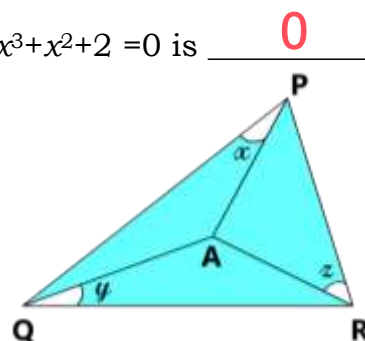
18. If $\cos \theta (\tan \theta + 2)(2 \tan \theta + 1) = a \sec \theta + b \sin \theta$, then $a+b$ is equal to **07**.

19. The number of real roots of the equation $x^4+x^3+x^2+2=0$ is 0.

20. In the adjoining figure, A is a point inside the triangle PQR, such that $AP = AQ = AR$.

Given $x + 2y = 109^\circ$ and $3x - y = 54^\circ$.

Then z (in degrees) is 20.



21. a, b, c are non-zero reals. Given $a + b + c = abc$ and $a^2 = bc$.

Then the minimum value of a^2 is 03.

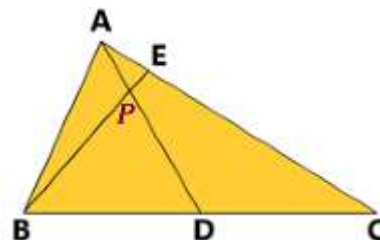
22. In the given figure (not drawn to scale)

$AC = 2AB$.

D, E are respectively points on BC and AC such that $\angle ABE = \angle CAD$.

If the triangle PBD is equilateral, and the measure of $\angle ABC$ is x° ,

then $x =$ 90.



23. The number of solutions x of the equation $(3|x| - 3)^2 = |x| + 7$ such that $\sqrt{x(x-3)}$ exists is 02.

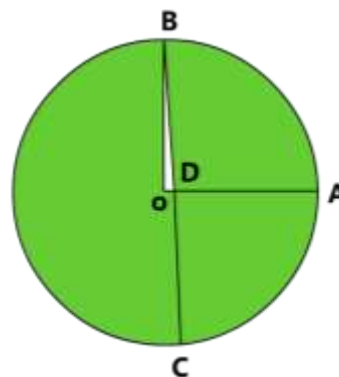
24. The difference between the fourth and first terms of a G.P. is 52. The sum of the first three terms is half of this difference. The n^{th} term of this G.P. just exceeds 2022. Then the value of n is 08.

25. In the adjoining figure, OA and OB are two perpendicular radii.

With A as centre and AO as radius, an arc is drawn to cut the circle at C.

BC cuts OA at D.

If $\angle ADC = x^\circ$, then $x =$ 75.



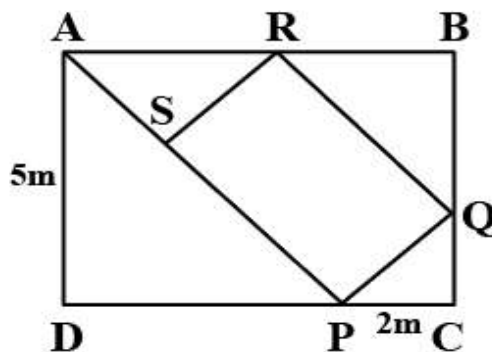
26. Three pipes p_1, p_2 and p_3 can fill a tank in 10 hours.

After working at it together for 2 hours, p_1 is closed and p_2 and p_3 can fill it in 16 hours. The time required by p_1 to fill the tank alone is

20 hours.

27. The least number which when divided by 8, 9, 12 and 15 leaves 1 as remainder *each* time is 361.
28. The sum of the digits of a two digit number is 15. If the digits are interchanged, the number of reverse digits is increased by 9. The original two digit number is 78.
29. The number of numbers divisible by 17 between 300 and 500 is 12.

30. ABCD is a non-standard billiards table. $AD = 5m$.
 A ball is projected from A along a line which makes 45° with AD.
 It bounces at P on DC, again bounces respectively at Q and R as shown and reaches the line AP at S.
 The total distance covered by the ball is $12\sqrt{2}m$



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