ASSOCIATION OF MATHEMATICS TEACHRS OF INDIA Screening Test – Bhaskara Contest (NMTC-- JUNIOR LEVEL—IX and X Grades)

Saturday, the 15th October 2022

<u>Note</u>:

- 1. Fill in the Response Sheet with your Name, Class and the Institution through which you appear, in the specified places.
- 2. Diagrams given are only Visual aids; they are not drawn to scale.
- 3. You may use separate sheets to do rough work.
- 4. Use of Electronic gadgets such as Calculator, Mobile Phone or Computer is not permitted.
- 5. Duration of the Test: 2 pm to 4 pm (2 hours).

01. ABCD is a trapezium in which AB is parallel to CD. If AB = 30 cm, CD = 15 cm, AD = 13 cm and BC = 14 cm, then the area of the trapezium (in square cm) is **c**) 252 **a**) 263 **d**) 293 **b**) 248 **02.** If a + b = 2, where a, b are real and $4^a + 4^b = 6$, then the numerical value of $2^{2(2a-1)} + 2^{2(2b-1)}$ is **c**) 36 **a**) 8 **b**) 12 **d**) 1 **03.** If $\left(x + \frac{1}{x}\right)^2 = 3$, then the value of $x^{33} + x^{23} + x^{27} + x^{17} + 2$ is **b**) 2 **c**) 0 **a**) 1 **d**) 4 **04.** The solution x of the equation $(5x)^x = 5^{5^5}$ is of the form a^b , then a+b is **a**) 5 **b**) 10 **c**) 20 **d**) 9 ABC is a right-angled isosceles triangle in which $\angle A = 90^{\circ}$. 05. D is a point on BC. Then $\frac{BD^2 + CD^2}{AD^2}$ is equal to **b**) 2 **c**) 3 **a**) 1 **d**) 4



08. The maximum number of equal pieces that can be cut from the two lengths of wire of 74 cm and 92 cm, with a piece of 2 cm left out of each (in cm) is

c) 3

c) 510

(in chi) is
a) 16 **b)** 18 **c)** 20 **d)** 14
09. The value of
$$\sqrt{\frac{343^4 + 49^8}{343^6 + 49^7}}$$
 is
a) 7 **b)** $\frac{1}{7}$ **c)** 49 **d)** $\frac{1}{49}$

10. In the adjoining figure, ABCDEFGH is a regular octagon. AB, ED are produced to meet at P. Then the measure of $\angle BPD$ is equal to

06. There are four equidistant parallel chords

The numerical value of $\frac{a^2 - d^2}{b^2 - c^2}$ is

shown in the figure.

a) 1

a) 508

of a circle whose lengths are a,b,c,d as

b) 2

b) 507

a)
$$45^{o}$$
 b) 40^{o} **c)** 30^{o}
11. If $4x^{2} + \frac{1}{x^{2}} = 2$, then the value of $8x^{3} + \frac{1}{x^{3}}$ is
a) 1 **b)** -1 **c)** 8



d) 0

12. For permissible real values of *x*, *y*, *z*, the value of the expression

$$\frac{(2x+5y-3z)^3 + (2x-5y+3z)^3 + 2x(2x+5y-3z)(2x-5y+3z)}{x^3}$$
 is
a) 16 **b)** 32 **c)** 64 **d)** 128

13. When $\theta \neq 0^{\circ}$, 90° the value of the expression

a) 1

$$\frac{(1 + \sec \theta + \tan \theta)(1 + \csc \theta + \cot \theta)}{1 + \tan \theta + \cot \theta + \sec \theta + \csc \theta}$$
is equal to
b) 2
c) -1
d) $\frac{1}{2}$

14. The number of real ordered pairs (x, y) which satisfy

15. *a*, *b* are natural numbers such that $\frac{a}{b} + \frac{b}{a} = a + b$; then

- **a**) a is odd and b is even.
- **b**) *a*, *b* are both even.
- c) Such natural numbers *a* and *b* do not exist.
- **d**) There is exactly one value of '*a*' and '*b*' which satisfy the equation.

Fill in the blanks:

16. The sum of all the roots of the equation $3^{\frac{x+2}{3x-4}} - 7 = 2\left(3^{\frac{5x-10}{3x-4}}\right)$ is _____.

18. If $\cos \theta (\tan \theta + 2)(2 \tan \theta + 1) = a \sec \theta + b \sin \theta$, then a+b is equal to _

07



- **23.** The number of solutions *x* of the equation $(3|x|-3)^2 = |x|+7$ such that $\sqrt{x(x-3)}$ exists is <u>02</u>.
- **24.** The difference between the fourth and first terms of a G.P. is 52. The sum of the first three terms is half of this difference. The n^{th} term of this G.P. just exceeds 2022. Then the value of n is _____.
- **25.** In the adjoining figure, OA and OB are two perpendicular radii. With A as centre and AO as radius, an arc is drawn to cut the circle at C. BC cuts OA at D. If $\angle ADC = x^{\circ}$, then $x = \underline{75}$.



26. Three pipes p₁, p₂ and p₃ can fill a tank in 10 hours.
After working at it together for 2 hours, p₁ is closed and p₂ and p₃ can fill it in 16 hours. The time required by p₁ to fill the tank alone is 20 hours.

- **27.** The least number which when divided by 8, 9, 12 and 15 leaves 1 as remainder *each* time is <u>361</u>.
- 28. The sum of the digits of a two digit number is 15. If the digits are interchanged, the number of reverse digits is increased by 9. The original two digit number is <u>78</u>.
- **29.** The number of numbers divisible by 17 between 300 and 500 is <u>12</u>.
- 30. ABCD is a non-standard billiards table. AD = 5m. A ball is projected from A along a line which makes 45° with AD. It bounces at P on DC, again bounces respectively at Q and R as shown and reaches the line AP at S. The total distance covered by the ball is <u>12sqrt2</u>m



-000-